Basic Radiation Calculations

The foundation of any calculation of the greenhouse effect was a description of how radiation and heat move through a slice of the atmosphere. At first this foundation was so shaky that nobody could trust the results. With the coming of digital computers and better data, scientists gradually worked through the intricate technical problems. A rough idea was available by the mid 1960s, and by the late 1970s, the calculations looked solid—for idealized cases. Much remained to be done to account for all the important real-world factors, especially the physics of clouds. (This genre of one-dimensional and two-dimensional models lay between the rudimentary, often qualitative models covered in the essay on “Simple Models of Climate” and the elaborate three-dimensional “General Circulation Models of the Atmosphere.”) Warning: this is the most technical of all the essays.

Early Attempts - The CO₂ greenhouse effect demonstrated (1950-1967) - Further uses of primitive calculations

Looking for a complete explanation of greenhouse warming, equations and all? For basic physics in one page see Wikipedia’s “idealized greenhouse model” article at http://en.wikipedia.org/wiki/Idealized_greenhouse_model. But you can only really understand the system by studying a textbook that explains how to run the equations on a large computer model that takes into account crucial factors like convection, clouds and ocean circulation. (See the Links Page, http://www.aip.org/history/climate/links.htm.)

“No branch of atmospheric physics is more difficult than that dealing with radiation. This is not because we do not know the laws of radiation, but because of the difficulty of applying them to gases.” — G.C. Simpson

In the 19th century, a few French physicists tried to calculate the energy balance of the planet as a whole, as if it were a rock hanging in front of a fire. They concluded (correctly, but more confidently than the physics of the time warranted) that Earth’s surface is considerably warmer than the surface of a bare rock would be at the same distance from the Sun. (See the essay on simple models for basic explanations.) Evidently physicists would have to take the atmosphere into account.

The simplest approach was to treat the atmosphere as if it were a single uniform layer, ignoring differences with height by using an average for the absorption and scattering of radiation. The result would be a “zero-dimensional” calculation for the Earth’s energy balance (or “energy budget”). The next step was one-dimensional models, figuring in variations with altitude. The physicist pretended that the atmosphere was the same everywhere around the planet, and looked

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1 Simpson (1928a), p. 70.
at how things changed through a column of air that reached from the ground to the top of the atmosphere. That meant calculating the flow of radiation up and down through the column. The problem of tracking rays layer by layer as gas molecules scattered or absorbed them was called “radiative transfer,” an elegant and difficult branch of theoretical physics.

One pioneer was Samuel P. Langley, who in the summer of 1881 climbed Mount Wilson in California, measuring the fall of temperature as the air got thinner. He inferred that without any air at all, the Earth’s temperature would be lower still—a direct demonstration of the so-called greenhouse effect. Langley followed up with calculations indicating that if the atmosphere did not absorb particular kinds of radiation, the ground-level temperature would drop well below freezing.\(^1\) Subsequent workers crafted increasingly refined calculations.

**Early Attempts**

In 1896 Svante Arrhenius went a step farther, grinding out a numerical computation of the radiation transfer for atmospheres with differing amounts of carbon dioxide gas (CO\(_2\)). He did the mathematics not just for one globally averaged column but for a set of columns, each representing the average for a zone of latitude. This two-dimensional or “zonal” model cost Arrhenius a vast amount of arithmetical labor, indeed far more than was reasonable. The data on absorption of radiation (from Langley) was sketchy, and Arrhenius’s theory left out some essential factors. On such a shaky foundation, no computation could give more than a crude hint of how changes in the amount of a gas could possibly affect climate.

The main challenge was to calculate how radiation passed through the atmosphere, and what that meant for the temperature at the surface. This was such a tough task that all by itself it became a minor field of research, tackled by scientist after scientist with limited success. Through the first half of the 20th century, workers refined the one-dimensional and two-dimensional calculations. To figure the Earth’s radiation budget they needed to fix in detail how sunlight heated each layer of the atmosphere, how this energy moved among the layers or down to warm the surface, and how the heat energy that was radiated back up from the surface escaped into space. Different workers introduced a variety of equations and mathematical techniques to deal with them, all primitive.\(^2\)

A landmark was work by George Simpson. He was the first to recognize that it was necessary to take into account, in detail, how water vapor absorbed or transmitted radiation in different parts of the spectrum. Moving from a one-dimensional model into two dimensions, Simpson also

\(^1\) As Langley later realized, his estimate went much too far below freezing, Langley (1884); see also Langley (1886).

\(^2\) The pioneer was W.H. Dines, who gave the first explicit model including infrared radiation upward and downward from the atmosphere itself, and energy moved up from the Earth’s surface into the atmosphere in the form of heat carried by moisture, Dines (1917); Hunt et al. (1986) gives a review.
calculated how the winds carry energy from the sun-warmed tropics to the poles, not only as the heat in the air’s gases but also as heat energy locked up in water vapor.\(^1\) Other scientists found that if they took into account how air movements conveyed heat up and down, even a crude one-dimensional model would give fairly realistic figures for the variation of temperature with height in the atmosphere.

Edward O. Hulburt worked out a pioneering example of such a “radiative-convective” model in 1931. Hulburt, a senior physicist at the U.S. Naval Research Laboratory, had a general interest in the structure of the upper atmosphere through his professional work on radio propagation and the ionosphere. Taking a brief excursion away from matters that interested the U.S. Navy, he carried out a one-dimensional calculation, using data on the absorption bands of radiation by CO\(_2\) and water vapor far more accurate than what was known in Arrhenius’s time. In his first attempt, Hulburt came up with an unreasonably high surface temperature. He realized that this was because he had considered only the transfer of radiation up through the atmosphere. If the lower atmosphere were actually so hot it would be unstable—the hot air would rise. He put in a crude measure for transfer of heat by convection. Now he got a figure that agreed with Arrhenius’s rough estimate that doubling or halving the amount of CO\(_2\) in the atmosphere would raise or lower the Earth’s surface temperature several degrees. Nobody took notice. Hulburt’s model was rudimentary (in fact his agreement with Arrhenius’s different but equally rudimentary model was largely a coincidence).\(^2\) Anyway a publication by a government physicist who worked on radio propagation was not the sort of thing meteorologists normally studied.

Most scientists saw no good reason to believe the hypothesis that adding or subtracting CO\(_2\) from the atmosphere could affect the climate. Unaware of the modern data that Hulburt had used, they believed that old laboratory measurements proved that the CO\(_2\) in the atmosphere already thoroughly blocked radiation in the part of the infrared spectrum where the heat absorption took place. Moreover, water vapor seemed to entirely block the same region of the spectrum. In short, the absorption was “saturated,” so that adding more gas could make no difference.

In 1938, when G.S. Callendar attempted to revive the theory of carbon dioxide greenhouse warming, he offered his own simple one-dimensional calculation (he apparently didn’t know

\(^1\) Simpson began with a gray-body calculation, Simpson (1928a); very soon after he reported that this paper was worthless, for the spectral variation must be taken into account, Simpson (1928b); 2-dimensional model (mapping ten degree squares of latitude and longitude): Simpson (1929a); a pioneer in pointing to latitudinal transport of heat by atmospheric eddies was Defant (1921); for other early energy budget climate models taking latitude into account, not covered here, see Kutzbach (1996), pp. 354-59.

\(^2\) Hulburt (1931). A still better picture of the vertical temperature structure, in mid-latitudes, was derived by Möller (1935). Whereas Arrhenius had left out convection, Hulburt left out water-vapor feedback, and neither had good absorption data. My thanks to S. Manabe for comments on this. As late as 1967, when Manabe carried through the correct convection calculation, he was unaware of Hulburt’s work: personal communication, Jan. 28, 2008.
about Hulburt’s work, which was not mentioned in Callendar’s notebooks until 1942). Dividing the atmosphere into twelve layers, Callendar tried to calculate how much heat radiation would come downward to the surface from each layer, and how the amount of radiation would change if more CO₂ were added. He concluded that in future centuries, as humanity put more gas into the air, the result could be a degree or so of warming. But this model too was obviously grossly oversimplified, ignoring many key interactions. Like Arrhenius but unlike Hulburt, Callendar did not take convection into account. Like Hulburt but unlike Arrhenius, Callendar did not figure in how warming could bring an increase in water vapor that could itself act as a greenhouse gas. Critics also pointed out that Callendar, like both Arrhenius and Hulburt, had not considered how a warmer and moister planet might have more clouds, which could reflect sunlight and maintain a cool temperature. His calculations failed to convince anyone.

Callendar himself pointed out in 1941 that the way CO₂ absorbed radiation was not so simple as every calculation so far had assumed. He assembled measurements, made in the 1930s, which showed that at the low pressures that prevailed in the upper atmosphere, the amount of absorption varied in complex patterns through the infrared spectrum. Hulburt had attempted to work through this, but even if the experts had noticed his publication they would have found it too primitive to prove anything. Nobody was ready to attempt the vast labor of computation needed to work out effects point by point through the spectrum, since the data were too sketchy to support firm conclusions anyway.

Solid methods for dealing with radiative transfer through a gas were gradually worked out in the first half of the century, less by meteorologists than by physicists and astronomers concerned with the way energy moves through the interiors and atmospheres of stars. The fundamental equations were published in 1906 by Karl Schwarzschild, much better known for his work on relativity and black holes, in a paper on “The Equilibrium of the Solar Atmosphere.” The enterprise culminated in 1950 in a magisterial text by the great astrophysicist Subrahmanyan Chandrasekhar, a panoply of exquisitely sophisticated equations and techniques. The full treatment of the problem of radiative transfer was so subtle and complex that Chandrasekhar regarded his monumental work as a mere starting-point. It was too subtle and complex for meteorologists. They mostly ignored the astrophysical literature and worked out their own shortcut methods, equations that they could reduce to a sequence of arithmetic exercises to get rough numerical results. What drove the work was a need for immediate answers to questions

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1 In 1942 Callendar did not take explicit note of Hulburt’s use of convection, but seems mainly to have been concerned that the calculation gave general support to the greenhouse theory. Callendar Papers (Climatic Research Unit, University of East Anglia, Norwich, UK) Box 2, Notebook 1942-IRS, p. 197. Copies kindly provided by James R. Fleming; see also Fleming (2007b), p. 70.

2 Callendar (1941); low-pressure resolution of details was pioneered by Martin and Baker (1932).

3 Schwarzschild (1906); Chandrasekhar (1950), which includes historical notes. Most of this work was first published in the *Astrophysical Journal*, a publication that meteorological papers of the period scarcely ever referenced.
about how infrared radiation penetrated the atmosphere—a subject of urgent interest to the military for signaling, sniping, reconnaissance, and later for heat-guided missiles.

The calculations could not be pushed far when people scarcely had experimental data to feed in. There were almost no reliable numbers on how water vapor, clouds, CO$_2$, and so forth each absorbed or scattered radiation of various kinds at various heights in the atmosphere. Laboratories began to gather good data only in the 1950s, motivated largely by Cold War military concerns.¹

Well into the 1960s, important work continued to be done with the “zero-dimensional” models that ignored how things varied from place to place and even with height in the atmosphere, models that calculated the radiation budget for the planet in terms of its total reflectivity and absorption. Those who struggled to add in the vertical dimension had to confront the subtleties of radiative transfer theory and, harder still, they had to figure how other forms of energy moved up and down: the spin of eddies, heat carried in water vapor, and so forth. A reviewer warned in 1962 that “the reader may boggle at the magnitude of the enterprise” of calculating the entire energy budget for a column of air—but, he added encouragingly, “machines are at hand.”²

The CO$_2$ Greenhouse Effect Demonstrated (1950-1967)

Digital computers were indeed being pressed into service. Some groups were exploring ways to use them to compute the entire three-dimensional general circulation of the atmosphere. But one-dimensional radiation models would be the foundation on which any grander model must be constructed—a three-dimensional atmosphere was just an assembly of a great many one-dimensional vertical columns, exchanging air with one another. It would be a long time before computers could handle the millions of calculations that such a huge model required. So people continued to work on improving the simpler models, now using more extensive electronic computations.

Most experts stuck by the old objection to the greenhouse theory of climate change—in the parts of the spectrum where infrared absorption took place, the CO$_2$ plus the water vapor that were already in the atmosphere sufficed to block all the radiation that could be blocked. In this “saturated” condition, raising the level of the gas could not change anything. But this argument was falling into doubt. The discovery of quantum mechanics in the 1920s had opened the way to an accurate theory for the details of how absorption took place, developed by Walter Elsasser during the Second World War. Precise laboratory studies during the war and after confirmed a new outlook. In the frigid and rarified upper atmosphere where the crucial infrared absorption takes place, the nature of the absorption is different from what scientists had assumed from the old sea-level measurements.

¹ For a review at the time, see Goody and Robinson (1951).
Take a single molecule of CO\(_2\) or H\(_2\)O. It will absorb light only in a set of specific wavelengths, which show up as thin dark lines in a spectrum. In a gas at sea-level temperature and pressure, the countless molecules colliding with one another at different velocities each absorb at slightly different wavelengths, so the lines are broadened considerably. With the primitive infrared instruments available earlier in the 20th century, scientists saw the absorption smeared out into wide bands. And they had no theory to suggest anything else. A modern spectrograph shows a set of peaks and valleys superimposed on each band, even at sea-level pressure, and in cold air at low pressure each band resolves into a cluster of sharply defined lines, like a picket fence. There are gaps between the H\(_2\)O lines where radiation can get through unless blocked by CO\(_2\) lines. All that showed up clearly in data compiled for the U.S. Air Force, drawing the attention of researchers to the details of the absorption, especially at high altitudes. Moreover, researchers working for the Air Force had become acutely aware of how very dry the air gets at upper altitudes—indeed the stratosphere has scarcely any water vapor at all. By contrast, CO\(_2\) is fairly well mixed all through the atmosphere, so as you look higher it becomes relatively more significant.\(^1\)

The main points could have been understood in the 1930s if scientists had looked at the greenhouse effect carefully (or if they had noticed Hulburt’s paper, which did take a careful look, or had pursued still earlier remarks by Arrhenius himself). But it was in the 1950s, with the new measurements in hand, that a few theoretical physicists realized the question was worth a long and careful new look. Most earlier scientists who looked at the greenhouse effect had treated the atmosphere as a slab, and only tried to measure and calculate radiation in terms of the total content of gas and moisture. But if you were prepared to tackle the full radiative transfer calculations, layer by layer, you would begin to see things differently. What if water vapor did entirely block any radiation that could have been absorbed by adding CO\(_2\) in the lower layers of the atmosphere? It was still possible for CO\(_2\) to make a difference in the thin, cold upper layers. Lewis D. Kaplan ground through some extensive numerical computations. In 1952, he showed that in the upper atmosphere the saturation of CO\(_2\) lines should be weak. Thus adding more of the gas would certainly change the overall balance and temperature structure of the atmosphere.\(^2\)

Neither Kaplan nor anyone else at that time was thinking clearly enough about the greenhouse effect to point out that it will operate regardless of the details of the absorption. The trick, again, was to follow how the radiation passed up layer by layer. Consider a layer of the atmosphere so high and thin that heat radiation from lower down would slip through. Add more gas, and the layer would absorb some of the rays. Therefore the place from which heat energy finally left the Earth would shift to a higher layer. That would be a colder layer, unable to radiate heat so efficiently. The imbalance would cause all the lower levels to get warmer, until the high levels became hot enough to radiate as much energy back out as the planet received. (For additional

\(^1\) The infrared database used to this day descends from data compiled by the Air Force Geophysical Laboratory at Hanscom Air Force Base, referred to in early radiative transfer textbooks as the "AFGL Tape." I am grateful to Raymond F. Pierrehumbert for clarifying important points in this section.

\(^2\) Arrhenius (1901b); Kaplan (1952).
explanation of the “greenhouse effect” see the essay on Simple Models.) Adding carbon dioxide will make for a stronger greenhouse effect regardless of saturation in the lower atmosphere.

(And actually, there is no saturation. The primitive infrared techniques of the laboratory measurements made at the turn of the century had given a misleading result. Studies from the 1940s on have shown that there is not nearly enough CO$_2$ in the atmosphere to block most of the infrared radiation in the bands of the spectrum where the gas absorbs it. Nor does water vapor bring complete saturation, in desert regions where the air is extremely dry.)

If anyone had put forth these simple arguments in the 1950s, they would not have convinced other scientists unless they were backed up by a specific, numerical calculation. The structure of the H$_2$O and CO$_2$ absorption bands at a given pressure and temperature did need to be considered in figuring just how much radiation is absorbed in any given layer. Every detail had to be taken into account in order to calculate whether adding a greenhouse gas would warm the atmosphere negligibly or by many degrees.

The challenge attracted physicist Gilbert N. Plass, who had already been doing lengthy calculations of infrared absorption in the atmosphere. He held an advantage over earlier workers, having not only the use of digital computers, but also better numbers, from spectroscopic measurements done by a group of experimenters he was collaborating with at the Johns Hopkins University. Military agencies supported their work for its near-term practical applications. But Plass happened to have read Callendar’s papers, and he was personally intrigued by the old puzzle of the ice ages and other climate changes.

Plass pursued a thorough set of one-dimensional computations, taking into account the structure of the absorption bands at all layers of the atmosphere. In 1956 he explained clearly, for the first time, that the water vapor absorption lines did not block the quite different CO$_2$ absorption spectrum, adding that there was scarcely any water in the upper atmosphere anyway. He further explained that although some of the CO$_2$ band itself was truly saturated, there were many additional minor spectral lines where adding more of the gas would increase the absorption of radiation. Moreover, spectral “lines” were not solid stripes, but smeared out in a way that depended on atmospheric pressure, with space on the sides where radiation could slip through. His arguments and calculations showed convincingly that adding or subtracting CO$_2$ could seriously affect the radiation balance, layer by layer through the atmosphere, and raise the temperature at ground level.

As for actual numbers, calculating multiple layers was a big step beyond Arrhenius, who with nothing but a pencil had to treat the atmosphere as a single slab. However, Plass took a step backward by looking at heating only at ground level. Arrhenius had figured in changes in the temperature of his slab of atmosphere, and the changes are fundamental to the greenhouse effect (by altering how heat radiates out into space at the top of the atmosphere). Like Arrhenius, then, if Plass wound up with reasonable sounding numbers it was more by luck than by getting all the physics right. In the end, Plass reported that the global temperature change if the level of CO$_2$ in
the atmosphere doubled (a number later dubbed “sensitivity”) would be a warming of nearly 4°C, that is, roughly 7°F.¹

From that point on, nobody could dismiss the greenhouse theory with the simple old objections about saturation and so forth. However, Plass’s specific numerical predictions for climate change made little impression on his colleagues, who saw at once that his calculation relied on unrealistic simplifications. Like Callendar, Plass had ignored a variety of important effects, such as the way a rise of global temperature might cause the atmosphere to contain more water vapor and more clouds. Like most others, he did not even consider exchange of heat between the Earth’s surface and the air. As one critic warned, Plass’s “chain of reasoning appears to miss so many middle terms that few meteorologists would follow him with confidence.” No matter; the entire topic of greenhouse warming was a minor speculation that seemed worth only an occasional glance.²

Around 1960 that changed abruptly. Stimulated in part by Plass, C.D. Keeling showed that the level of CO₂ in the atmosphere was in fact rising fast, undoubtedly due to humanity’s emissions. Fritz Möller now tried to follow up on Plass’s attempt with a better calculation, and came up with a rise of 1.5°C for doubled CO₂. But when Möller took into account the increase of absolute humidity with temperature, by holding relative humidity constant, his calculations showed a massive feedback. A rise of temperature increased the capacity of the air to hold moisture (the “saturation vapor pressure”), and the result was an increase of absolute humidity. More water vapor in the atmosphere redoubled the greenhouse effect—which would raise the temperature still higher, and so on. Möller discovered “almost arbitrary temperature changes.” That seemed unrealistic, and he took recourse in a calculation that a mere 1% increase of cloudiness (or a 3% drop in water vapor content) would cancel any temperature rise that a 10% increase in CO₂ might bring. He concluded that “the theory that climatic variations are affected by variations in the CO₂ content becomes very questionable.” Indeed his entire method for getting a global temperature, like Plass’s and Arrhenius’s, was later shown to be seriously flawed.³

Yet most research begins with flawed theories, which prompt people to make better ones. Some scientists found Möller’s calculation fascinating. Was the mathematics trying to tell us something

¹ Plass (1956a) [reprinted with commentary at https://www.americanscientist.org/article/carbon-dioxide-and-the-climate, q.v. for biographical material on Plass by R. Fleming, also reprinted, with extensive commentary on radiative transfer, in Archer and Pierrehumbert (2011)]; Plass (1956d); see also Plass (1956b); Plass (1956c); Möller (1957) reviews the state of understanding as of about 1955.


³ Möller (1963), quote p. 3877.
truly important? It was a disturbing discovery that a simple calculation (whatever problems it might have in detail) could produce a catastrophic outcome. Huge climate changes, then, were at least theoretically conceivable. Moreover, it was now more clear than ever that modelers would have to think deeply about feedbacks, such as changes in humidity and their consequences.

Clouds were the worst problem (and always would be). Obviously the extent of the planet’s cloud cover might change along with temperature and humidity. And obviously even the simplest radiation balance calculation required a number that told how clouds reflect sunlight back into space. The albedo (amount of reflection) of a layer of stratus clouds had been measured at 0.78 back in 1919, and for decades this was the only available figure. Finally around 1950 a new study found that for clouds in general, an albedo of 0.5 was closer to the mark. When the new figure was plugged into calculations, the results differed sharply from all the preceding ones (in particular, the flux of heat carried from the equator to the poles turned out some 25% greater than earlier estimates).  

Worse, besides the average albedo you needed to know the amount and distribution of cloudiness around the planet, and for a long time people had only rough guesses. In 1954, two scientists under an Air Force contract compiled ground observations of cloudiness in each belt of latitude. Their data were highly approximate and restricted to the Northern Hemisphere, but there was nothing better until satellite measurements came along in the 1980s. And all that only described clouds as currently observed, not even considering how cloudiness might change if the atmosphere grew warmer.

Getting a proper calculation for the actions of water vapor seemed all the more important after Möller’s discovery that a simple model with water vapor feedback could show catastrophic instability. No doubt his model was over simple, but what might the real climate actually do? Partly to answer that question, in the mid 1960s Syukuro Manabe with collaborators developed the first approximately realistic model. They began with a one-dimensional vertical column of atmosphere, averaged over a zone of latitude or over the entire globe. In this column of air they modeled subtle but important features. They continued to assume constant average relative humidity. But in layers of air at different altitudes they calculated different balances between the way clouds trapped radiation and warmed the planet, or reflected sunlight back into space and cooled it. These balances would change when global warming added moisture to the air.

More important, with encouragement from Möller, Manabe went beyond Möller himself by including a calculation of how updrafts of air carry heat up from the surface. That was a crucial step beyond trying to calculate surface temperatures by considering only the energy balance of radiation reaching and leaving the surface. Manabe understood that a significant amount of energy leaves the surface not as radiation but through convection, the rising of warm air. Most of the heat is carried as latent energy in water vapor, for example in the columns of humid air that climb into thunderclouds. The energy eventually reaches thin levels near the top of the atmosphere, and is radiated out into space from there. If the surface got warmer, convection

\[1\] Houghton (1954). Houghton did not discuss whether an important part of the heat flux might be carried by the oceans.

\[2\] Published only in an Air Force contract report, Telegdas and London (1954).
would carry more heat up. Møller’s calculations, and all the rest back to Arrhenius (aside from Hulburt’s overlooked paper), had been flawed because they failed to take account of this basic process.¹

In the numbers printed out for Manabe’s model in 1964, some of the general characteristics, although by no means all, looked rather like the real atmosphere.² By 1966, after further improvements in collaboration with Richard Wetherald, Manabe was ready to see what might result from raising the level of CO₂. The result was the first somewhat convincing calculation of greenhouse effect global warming. The movement of heat through convection kept the temperature from running away to the extremes Møller had seen. Overall, the new model predicted that if the amount of CO₂ doubled, temperature would rise a plausible 2°C.³ In the view of many experts, this widely noted calculation (to be precise: the Manabe-Wetherald one-dimensional radiative-convective model) gave the first reasonably solid evidence that greenhouse warming really could happen.

Many gaps remained in radiation balance models. One of the worst was the failure to include dust and other aerosols. It was impossible even to guess whether they warmed or cooled a given latitude zone. That would depend on many things, such as whether the aerosol was drifting above a bright surface (like desert or snow) or a dark one. Worse, there were no good data nor reliable physics calculations on how aerosols affected cloudiness.⁴ One attempt to attack the problem came in 1971 when S. I. Rasool and Stephen Schneider of NASA worked up their own globally averaged radiation-balance model, with fixed relative humidity, cloudiness, etc. The pioneering feature of their model was an extended calculation for dust particles. They found that the way humans were putting aerosols into the atmosphere could significantly affect the balance of radiation. The consequences for climate could be serious—an enormous increase of pollution, for example, might cause a dire cooling—although they could not say for sure. (This paper has been

¹ The earlier workers mostly assumed that the flux of sensible and latent heat would be fixed. Arrhenius further had inadequate data for water vapor absorption, while Callendar and Plass as well as Hulburt left out the water vapor feedback altogether. I thank S. Manabe for clarifying these matters.

² Manabe and Strickler (1964); see also Manabe et al. (1965); the 1965 paper was singled out by National Academy of Sciences (1966), see pp. 65-67 for general discussion of this and other models. Manabe and Broccoli (2020); Manabe, interview by Paul Edwards, Session I, 1998, AIP, online at https://www.aip.org/history-programs/niels-bohr-library/oral-histories/32158-1.

³ “Our model does not have the extreme sensitivity... adduced by Møller.” Manabe and Wetherald (1967), quote p. 241; the earlier paper, Manabe and Strickler (1964), used a fixed vertical distribution of absolute humidity, whereas the 1967 work more realistically had moisture content depend upon temperature by fixing relative humidity, a method adopted by subsequent modelers.

⁴ The pioneer radiation balance model incorporating aerosols was Freeman and Liou (1979); for cloudiness data they cite Telegdas and London (1954).
cited as a prediction of an imminent ice age. In fact it was only an admittedly very rough calculation of possible effects of extremely large human inputs.) They also calculated that under some conditions a planet could suffer a “runaway greenhouse” effect. As increasing warmth evaporated ever more water vapor into the air, the atmosphere would turn into a furnace like Venus’s. Fortunately our own planet was apparently not at risk.¹

Further Uses of Primitive Calculations

By the 1970s, thanks partly to such one-dimensional studies, scientists were starting to see that the climate system was so rich in feedbacks that a simple set of equations might not give an approximate answer, but a completely wrong one. The best way forward would be to use a model of a vertical column through the atmosphere as the basic building-block for fully three-dimensional models. Nevertheless, through the 1970s and into the 1980s, a number of people found uses for less elaborate models.

For understanding the basic greenhouse effect itself, one-dimensional radiative-convective models remained central. Treating the entire planet as a single column of air allowed researchers to include intricate details of radiation and convection processes without needing an impossible amount of computing time.² These models were especially useful for checking the gross effects of influences that had not been incorporated in the bigger models. As late as 1985, this type of schematic calculation gave crucial estimates for the greenhouse effects of a variety of industrial gases (collectively they turned out to be even more important than CO₂).³

Another example was a 1978 study by James Hansen’s NASA group, which used a one-dimensional model to study the effects on climate of the emissions from volcanic eruptions. They got a realistic match to the actual changes that had followed a 1968 explosion. In 1981, the group got additional important results by investigating various feedback mechanisms while (as usual) holding parameters like relative humidity and cloudiness fixed at a given temperature. Taking into account the dust thrown into the atmosphere by volcanic eruptions plus an estimate of solar activity variations, they got a good match to modern temperature trends.⁴

Primitive one-dimensional models were also valuable, or even crucial, for studies of conditions far from normal. Various groups used simple sets of equations to get a rough picture of the basic physics of the atmospheres of other planets such as Mars and Venus. When they got plausible rough results for the vastly different conditions of temperature, pressure, and even chemical composition, that confirmed that the basic equations were broadly valid. Primitive models could

¹ Rasool and Schneider (1971). For more on this paper, see the essay on aerosols.
² Ramanathan and Coakley (1978) gives a good review, see p. 487.
³ Ramanathan et al. (1985).
⁴ Hansen et al. (1978); Another pioneer radiation balance model incorporating aerosols was Freeman and Liou (1979); Hansen et al. (1981).
also give an estimate of how the Earth’s own climate system might change if it were massively clouded by dust from an asteroid strike, or by the smoke from a nuclear war.

Other scientists worked with zonal energy-balance models, taking the atmosphere’s vertical structure as given while averaging over zones of latitude. These models could do quick calculations of surface temperatures from equator to pole. They were useful to get a feeling for the effects of things like changes in ice albedo, or changes in the angle of sunlight as the Earth’s orbit slowly shifted. More complex two-dimensional models, varying for example in longitude as well as latitude, were becoming useful chiefly as pilot projects and testing-grounds for the far larger three-dimensional “general circulation models” (GCMs). Even the few scientists who had access to months of time on the fastest available computers sometimes preferred not to spend it all on a few gigantic runs. Instead they could do many runs of a simpler model, varying parameters in order to get an intuitive grasp of the effects.

To give one example of many, a group at the Lawrence Livermore Laboratory in California used a zonal model to track how cloud cover interfered with the heat radiation that escaped from the Earth. The relationship changed when they doubled the amount of CO$_2$. They traced the cause of the change to variations in the height and thickness of clouds at particular latitudes. As one expert pointed out, “it is much more difficult to infer cause-effect relationships in a GCM.”

A GCM’s output was hundreds of thousands of numbers, a simulated climate nearly as complicated and inscrutable as the Earth’s climate itself.

Simple models also served as testbeds for “parameterizations”—the simple equations or tables of numbers that modelers built into GCMs to represent averages of quantities they lacked the power to compute for every cubic meter of atmosphere. You could fiddle with details of physical processes, varying things in run after run (which would take impossibly long in a full-scale model) to find which details really mattered. Still, as one group admitted, simple models were mostly useful to explore mechanisms, and “cannot be relied upon for quantitative discussion.”

The basic models could still be questioned at the core. Most critical were the one-dimensional radiative-convective models for energy transfer through a single column of the atmosphere, which were often taken over directly for use in GCMs. In 1979, Reginald Newell and Thomas Dopplick pointed to a weakness in the common GCM prediction that increased CO$_2$ levels would bring a large greenhouse warming. Newell and Dopplick noted that the prediction depended crucially on assumptions about the way a warming atmosphere would contain more of that other greenhouse gas, water vapor. With a simple calculation of the energy balance in the tropics that suggested the accepted climate models might overestimate the greenhouse effect on temperature

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2 GCMs were “typically as complicated and inscrutable as the Earth’s climate...” simple models “cannot be relied upon,” Washington and Meehl (1984), p. 9475.
by an order of magnitude, the pair cast doubt on whether scientists understood the greenhouse effect at all.¹

In 1980 a scientist at the U.S. Water Conservation Laboratory in Arizona, Sherwood Idso, joined the attack on the models. In articles and letters to several journals, he asserted that he could determine how sensitive the climate was to additional gases by applying elementary radiation equations to some basic natural “experiments.” One could look at the difference in temperature between an airless Earth and a planet with an atmosphere, or the difference between Arctic and tropical regions. Since these differences were only a few tens of degrees, like Newell and Dopplick he calculated that the smaller perturbation that came from doubling CO₂ must cause only a negligible change, a tenth of a degree or so.²

Stephen Schneider and other modelers counterattacked. They showed that Idso, Newell, and Dopplick were misusing the equations—indeed their conclusions were “simply based upon various violations of the first law of thermodynamics.” Newell and Dopplick had ignored, among other things, the crucial transfer of heat from the tropics toward the poles, and Idso’s approach did not even conserve energy. Refusing to admit error, Idso got into a long technical controversy with modelers, which on occasion descended into personal attacks. It was the sort of conflict that an outsider might find arcane, almost trivial. But to a scientist, raising doubts about whether you were making scientific sense or nonsense aroused the deepest feelings of personal value and integrity. (In later years Idso joined the climate “deniers,” accepting funds from fossil fuel corporations and arguing that restrictions on their emissions would be foolish—although he switched his grounds for making that argument.)³

Most experts remained confident that the radiation models used as the basis for GCMs were fundamentally sound, so long as they did not push the models too far. The sets of equations used in different elementary models were so different from one another, and the methods were so different from the elaborate GCM computations, that they gave an almost independent check on

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¹ Newell and Dopplick (1979).
² Idso (1980); Idso (1987).
³ Schneider et al. (1980), see pp. 7-8; Ramanathan (1981) (with the aid of W. Washington’s model); National Research Council (1982); Cess and Potter (1984), quote p. 375; Schneider (1984); Webster (1984); for further references, see Schneider and Londer (1984); cf. reply, Idso (1987); the controversy is reviewed by Frederick M. Luther and Robert D. Cess in MacCracken and Luther (1985b), App. B, pp. 321-34; see also Gribbin (1982), pp. 225-32; Oreskes et al. (2008b), pp. 130-131. Idso later argued, notably in “The Greening of Planet Earth” (video, 1991) funded by the Western Fuels Association, that because CO₂ can fertilize plants, emissions are beneficent.
one another. Where all of the approaches agreed, the results were very probably robust—and where they didn’t agree, well, everyone would have to go back to their blackboards.¹

The most important such comparison of various elementary models and GCMs was conducted for the U.S. government in 1979 by a panel of the National Academy of Sciences, chaired by Jule Charney.² The panel’s report announced that the simple models agreed quite well with one another and with the GCMs; simple one-dimensional radiative-convective models, in particular, showed a temperature increase only about 20% lower than the best GCMs. That gave a new level of confidence in the predictions, from every variety of model, that doubled CO₂ would bring significant warming. As a 1984 review explained, the various simple radiative-convective and energy-balance models all continued to show remarkably good agreement with one another: doubling CO₂ would change temperature within a range of roughly 1.3 to 3.2°C (that is, 2.3 to 5.8°F). And that was comfortably within the range calculated by the big general circulation models (with their wide variety of assumptions about feedbacks and other conditions, these gave a wider spread of possible temperatures).³

Much remained to be done before anyone could be truly confident of these findings. For example, it was not until 2009 that satellite measurements showed definitively that Manabe’s idea of simply holding relative humidity constant as the temperature increased did describe quite exactly how the global atmosphere behaved.⁴ The problem of cloud feedback, in particular—which the Charney Panel had singled out as one of the “weakest links”—could never be solved exactly, although great efforts at data-gathering and theoretical analysis did bring steady improvements. Simple models would continue to be helpful for investigating such parameters. Otherwise the Charney Panel’s report marked the successful conclusion of the program of basic radiation calculations. While they would still provide useful guidance for specialized topics, in future their main job would be making a foundation for the full apparatus of the general circulation models.

Unfortunately, having the correct theory was not the same as calculating the precise effect of CO₂ on infrared radiation throughout an atmosphere of bewildering complexity and constant change. State-of-the art computer models diverged significantly in their climate projections, and a 1993 survey found that a large part of the variation came from differences in their radiation calculations. The problem was, although you could make a quite accurate calculation by considering every spectral line and the local temperature and so forth at every level, to do that at every point around the globe, and again and again for each step forward in time, was beyond the capacity of the fastest computers. Modelers had to fall back on shorthand estimates that

¹ Schneider and Dickinson (1974), p. 489; North et al. (1981), quote p. 91, see entire articles for review.
⁴ Dessler et al. (2008).
summarized processes with a few approximate numbers (parameters). In 2018 an expert admitted that “substantial differences still exist in these parameterizations.... The lack of progress over the past 25 years is disconcerting. The spread in model calculations of CO\(_2\) forcing does not represent an uncertainty in radiative transfer theory, but rather the failure to implement that theory consistently.”

This set of essays does not attempt to cover developments from the 1980s forward in radiation models, a matter of increasingly sophisticated technical detail. Some related later developments in the basic structure of computer models are covered in the essay on simple models.

A final note: All the work described in this essay relied deeply on other kinds of research, the lifework of hundreds of other scientists over the course of generations. There was the fundamental task of understanding exactly how molecules of water, CO\(_2\) and so forth in the atmosphere absorb radiation in different parts of the spectrum, and in particular how this varies with the temperature and pressure of the gas. I have mentioned how theorists applied quantum mechanics to calculate answers, while others made laboratory measurements to check whether the theorists were coming up with the right numbers. This task, pursued by many, was essentially finished in the 1960s. That was only a beginning It was also necessary to measure the radiation coming in from the Sun throughout the spectrum. Accurate instruments for the infrared became available in the 1950s, and this work too was essentially finished in the 1960s. The final step, as yet far from completion, is to measure the actual temperature and concentration of each molecule at each point in the atmosphere— including methane, ozone, aerosols and much more. As such data improve, so will the calculated models of climate. This task engages not only instrument builders (starting in the 1950s with balloons and sounding rockets, then extending to satellites) but also theorists, who have devised hundreds of ingenious techniques for taking measurements and analyzing the results. No single scientist or team could add more than a few pieces to the immense jigsaw puzzle. And so the enterprise would have bogged down without an ongoing cooperative effort to coordinate, verify, calibrate and exchange data. Scientists spent countless hours on such work, collaborating in organizations unknown to almost everyone else, such as the Radiation Commission of the International Union of Geodesy and Geophysics. An entire book, albeit a tedious one, could be written about these various efforts, unsung but essential, which laid a foundation for everything else.\(^2\)

Related: General Circulation Models of the Atmosphere

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\(^1\) Cess et al. (1993), Soden et al. (2018).